

# Experimental aspects of jet physics in ep collisions

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CTEQ / POETIC 2016 – Temple University

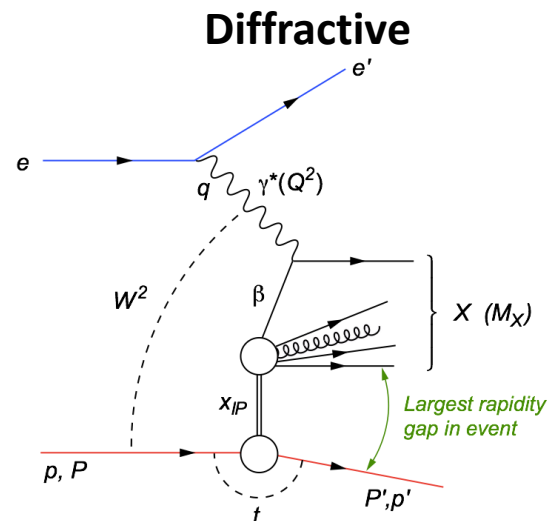
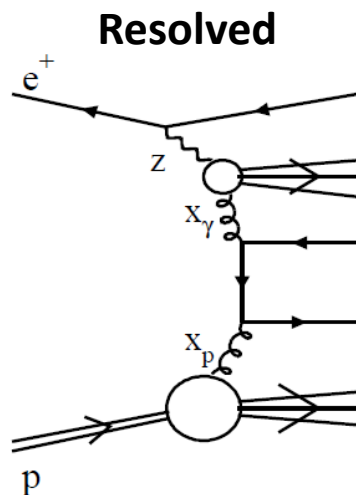
# Introduction

- Basics of jet finding in ep
- Example application: Accessing gluons with di-jets
- Limits of jet applicability: How low in transverse momentum can we go?

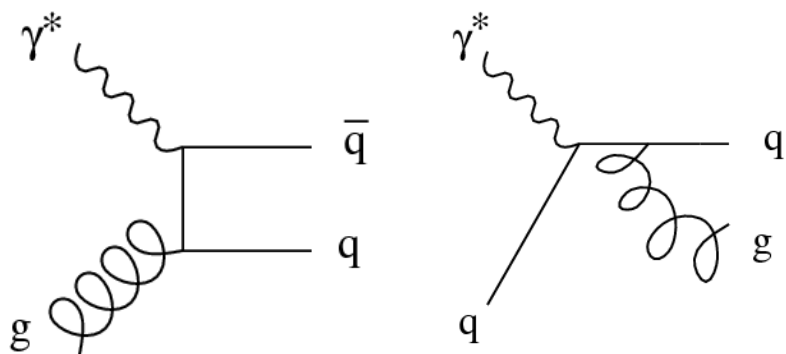
# Simulation Details / Particle Cuts

- Electron – Proton events generated using PYTHIA
- Full energy eRHIC: 20 x 250 GeV ( $\sqrt{s} = 141$  GeV)
- Cut on inelasticity:  $0.01 \leq y \leq 0.95$
- Particles used in jet finding:
  - Stable
  - $p_T \geq 250$  MeV
  - $\eta \leq 4.5$
  - Parent cannot originate from scattered electron

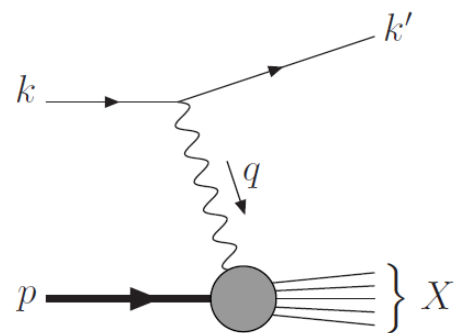
# Subprocesses



## Photon-Gluon Fusion & QCD-Compton

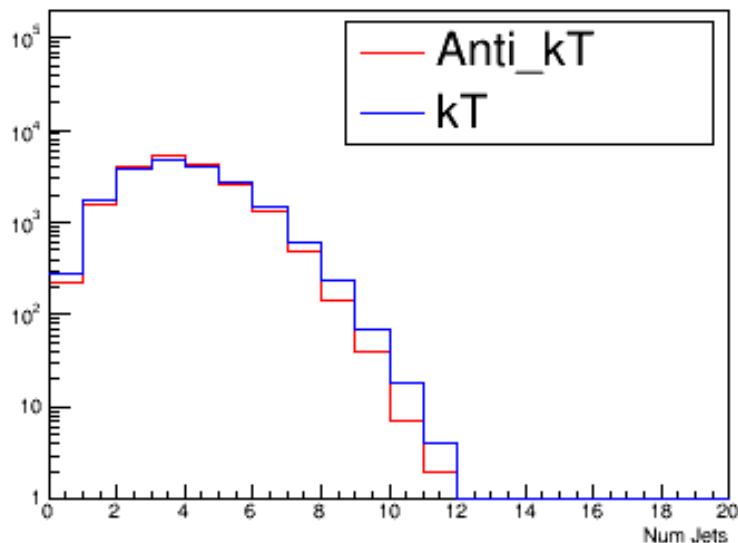


## DIS



# Jet Basics: Algorithm

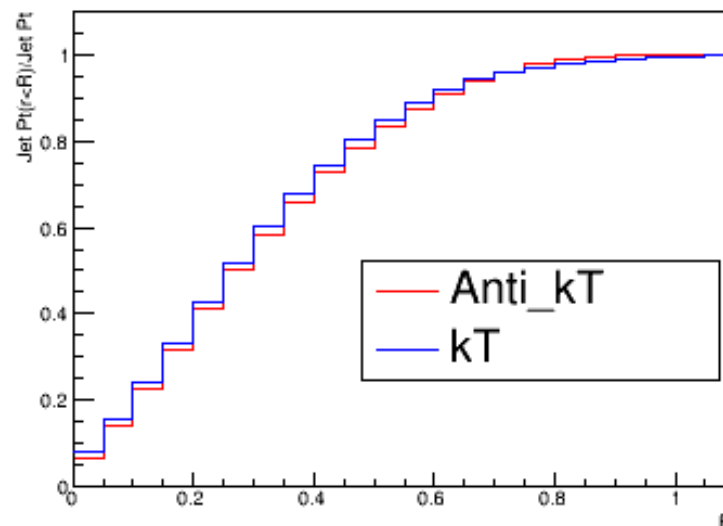
Number of Jets



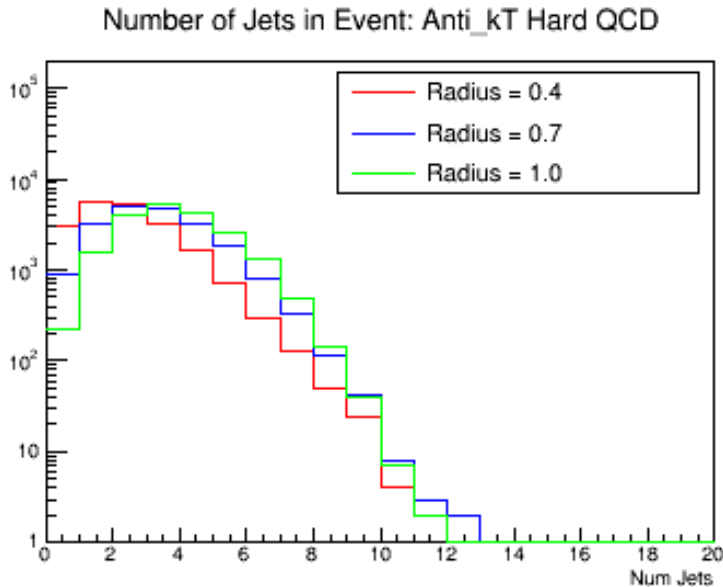
- Parameters: Radius = 1, Min  $p_T$  = 1.0 GeV, Resolved Processes
- Look at number of jets in event and jet profile (amount of jet  $p_T$  in certain radius)
- $k_T$  and anti- $k_T$  show very similar behavior

- Many jet clustering algorithms available
- Compare  $k_T$  and anti- $k_T$  (widely used at hadron colliders)
- Infrared and collinear safe at all orders

Jet Profile

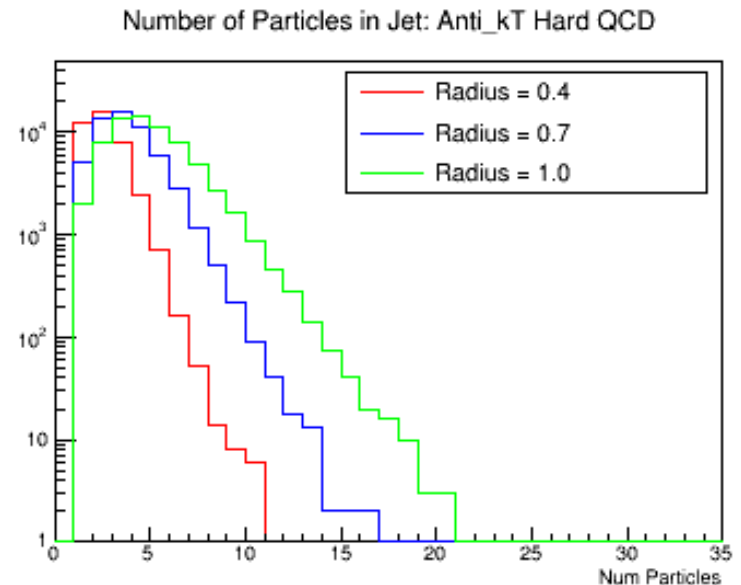


# Jet Basics: Radius



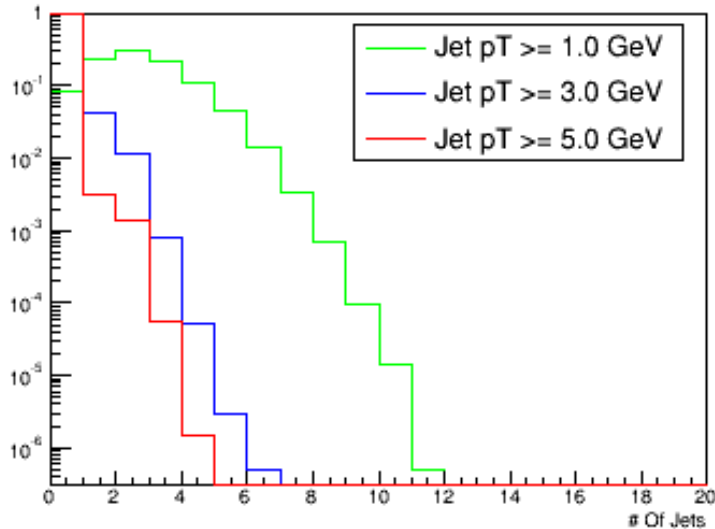
- Parameters: Min  $p_T = 1.0$  GeV, Resolved processes
- Larger radii result in more found jets as well as more particles in jet

- For anti- $k_T$  algorithm the radius parameter determines the distance at which particles can be grouped together
- Sets the effective size of the jet

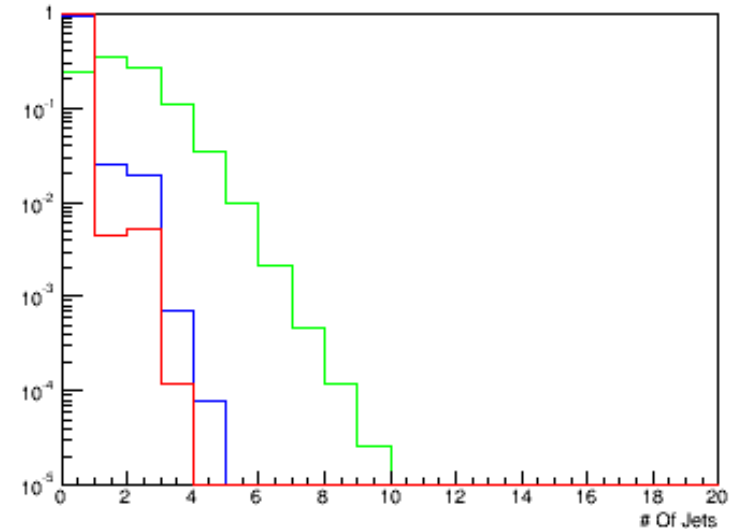


# Jet Multiplicity: $Q^2 = 0.01 - 0.1 \text{ GeV}^2$

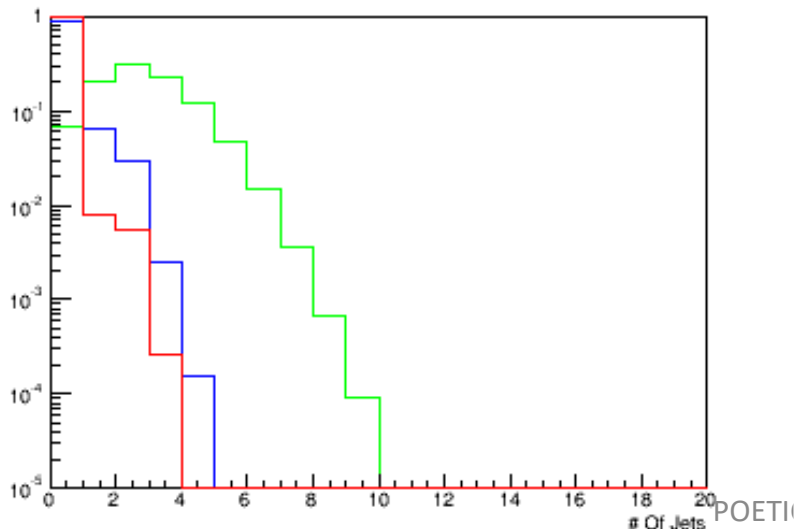
# Jets: Resolved Processes



# Jets: QCD



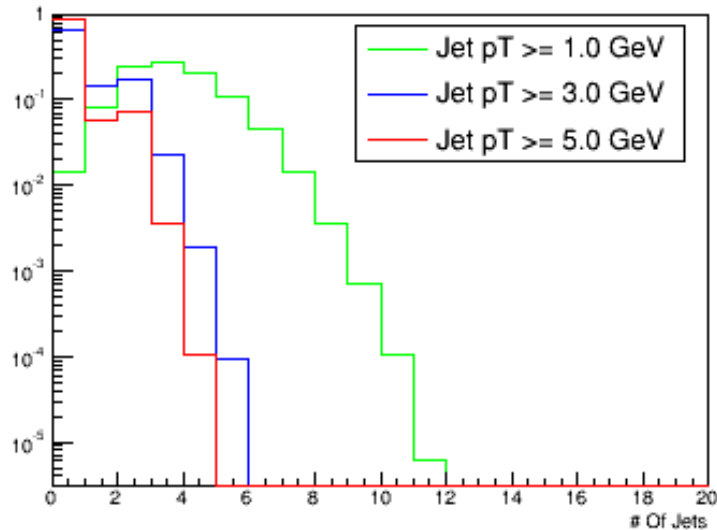
# Jets: PGF



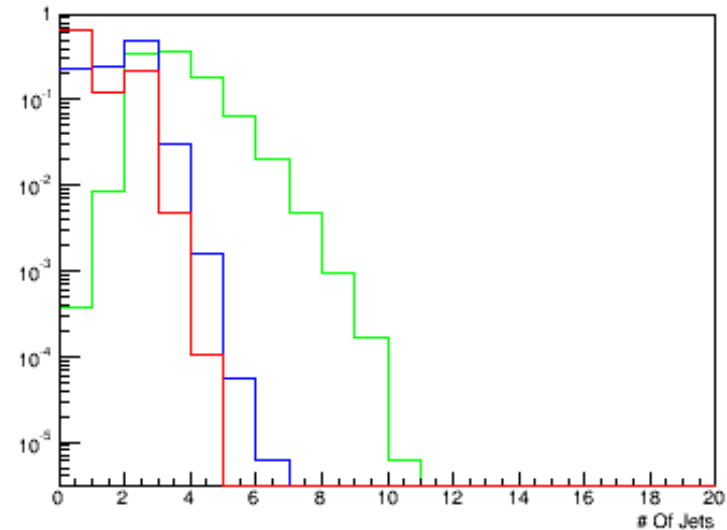
- Percentage of events with a certain number of found jets for different minimum allowed jet  $p_T$ s
- See a decrease in number of jets with increasing minimum jet  $p_T$
- Jet  $p_T$  of 1 GeV may not be well described theoretically
- Each curve normalized to unity

# Jet Multiplicity: $Q^2 = 10 - 100 \text{ GeV}^2$

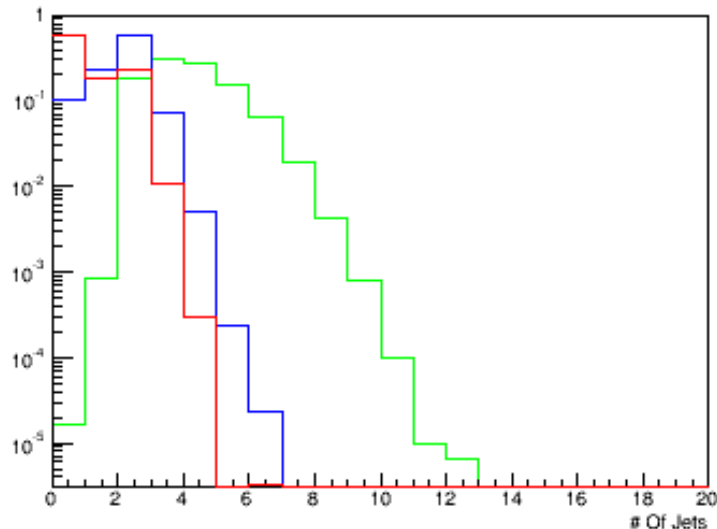
# Jets: Resolved Processes



# Jets: QCD



# Jets: PGF

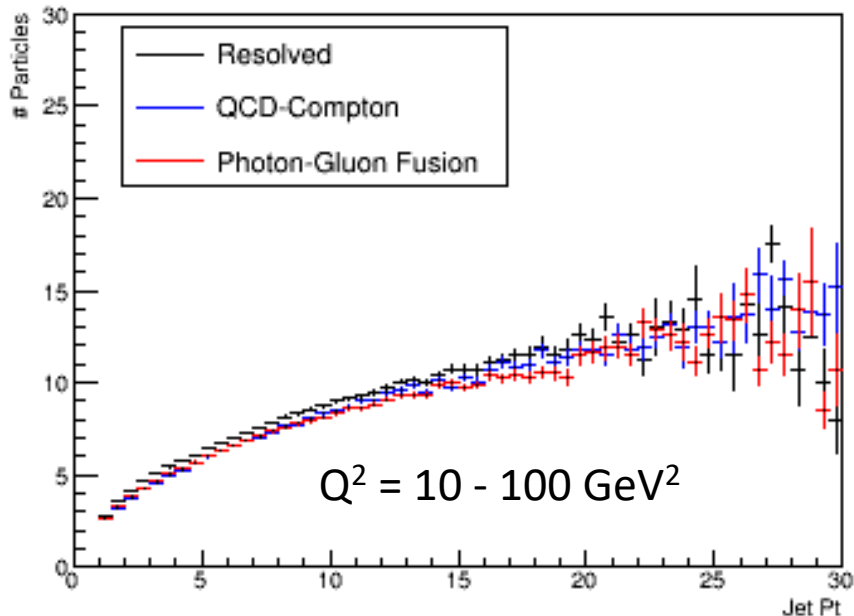


- Same as above for higher  $Q^2$  range
- Note the increase in percentage of events containing jets



# Jet Particle Multiplicity

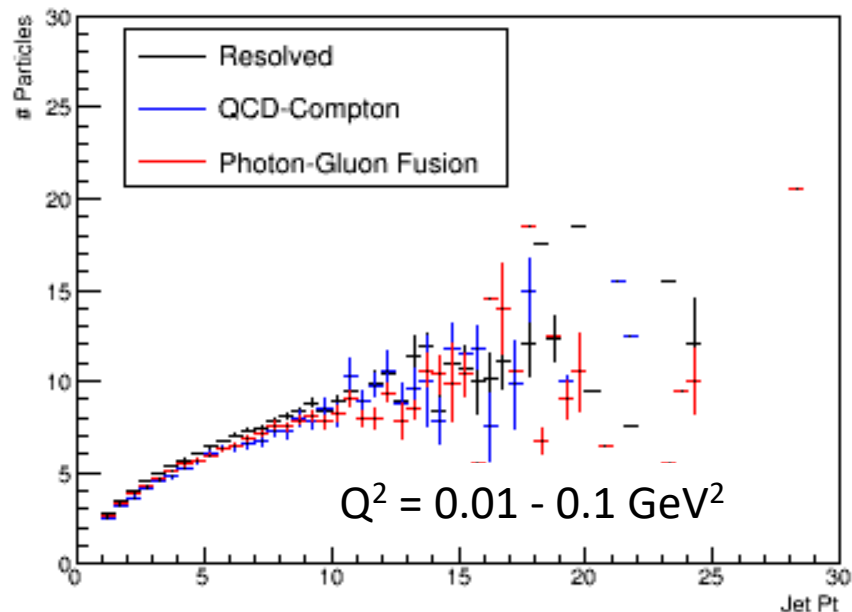
Number of Particles in Jet Vs Jet Pt



- No dependence on  $Q^2$  or subprocess
- How few particles can be in jet before it doesn't make sense to call the object a jet?

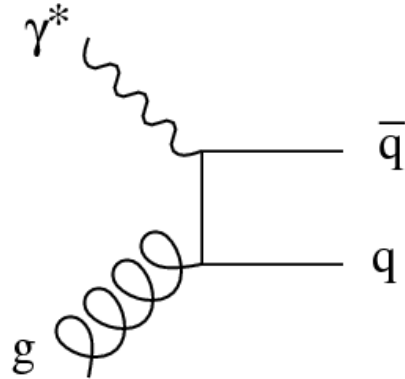
- Look at the average number of particles in jet as a function of jet  $p_T$
- All stable particles (charged and neutral) are counted

Number of Particles in Jet Vs Jet Pt



# Accessing Gluons with Di-jets

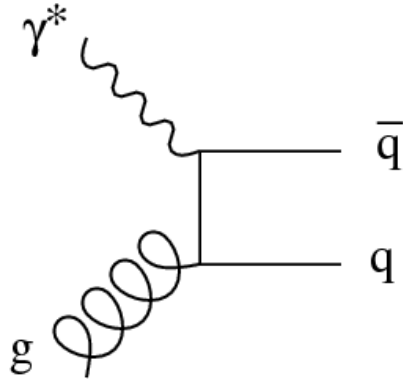
## Photon-Gluon Fusion



- Gluons can be probed in DIS via the higher-order photon gluon fusion process

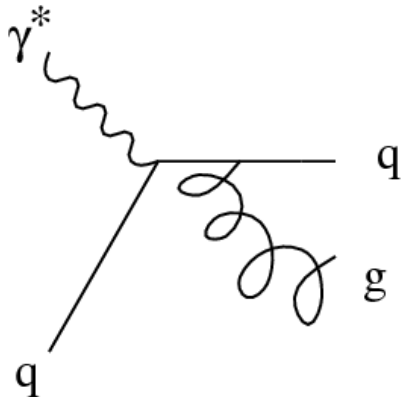
# Accessing Gluons with Di-jets

## Photon-Gluon Fusion



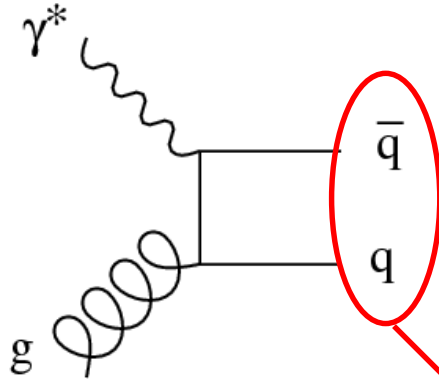
- Gluons can be probed in DIS via the higher-order photon gluon fusion process
- Also have the QCD – Compton process which probes quarks at the same order

## QCD – Compton

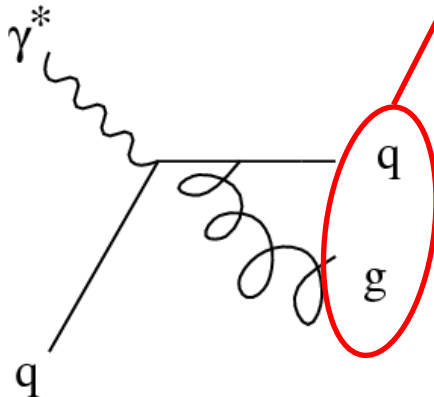


# Accessing Gluons with Di-jets

## Photon-Gluon Fusion



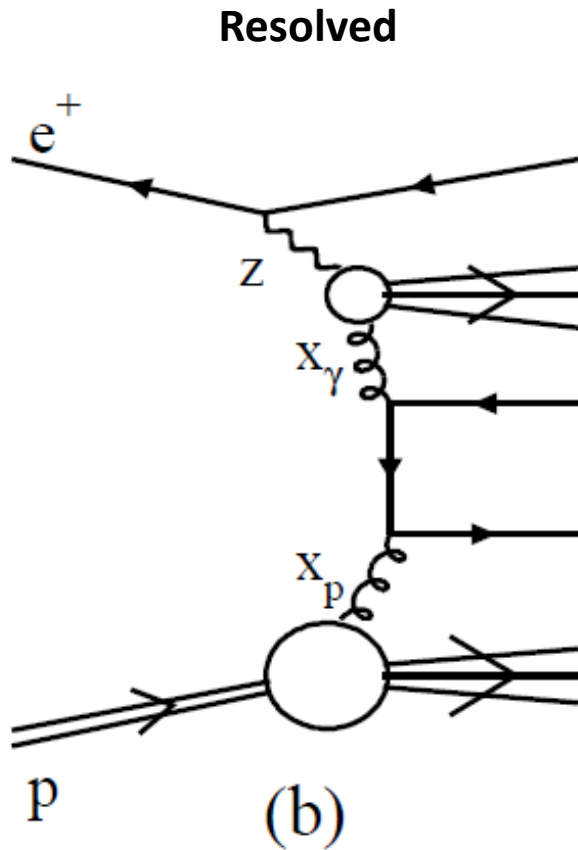
## QCD – Compton



- Gluons can be probed in DIS via the higher-order photon gluon fusion process
- Also have the QCD – Compton process which probes quarks at the same order
- Both processes produce 2 angularly separated hard partons  $\rightarrow$  Di-jet

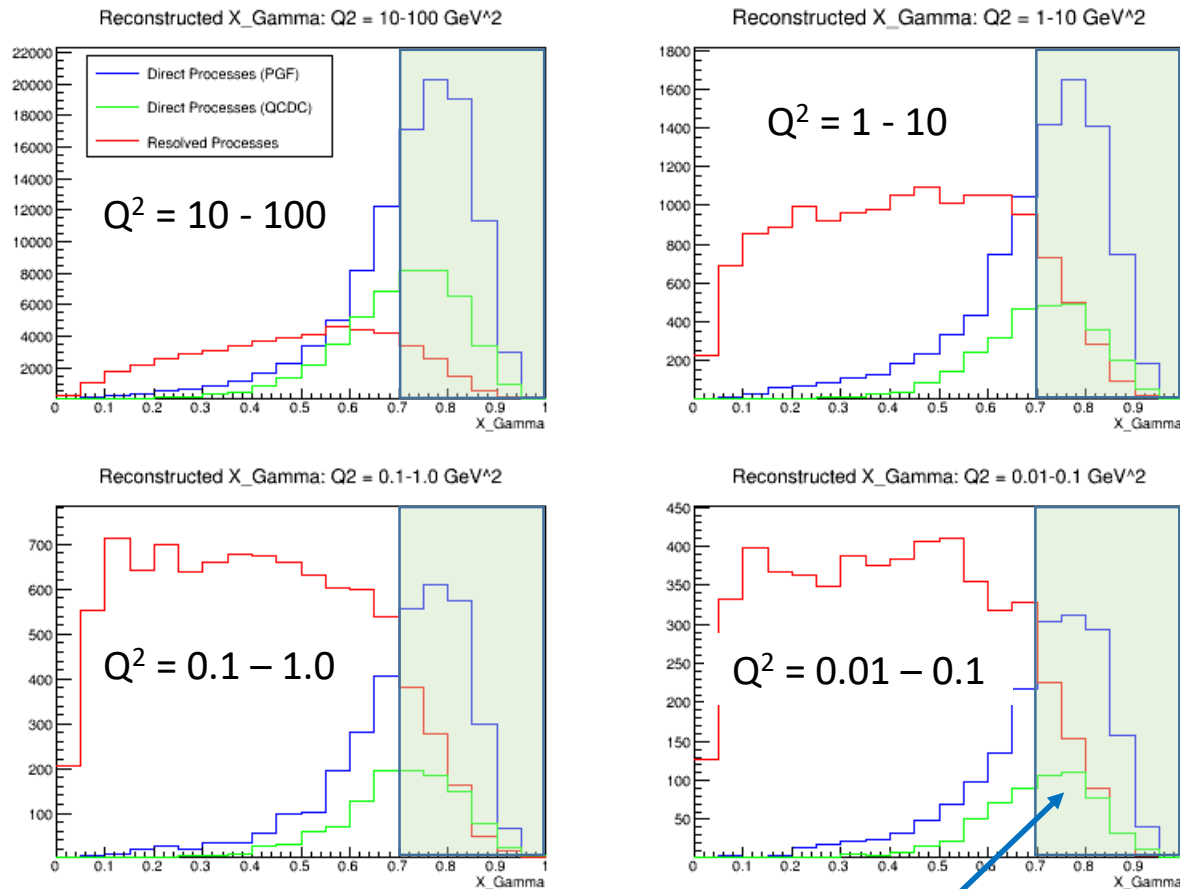
# Accessing Gluons with Di-jets

- Gluons can be probed in DIS via the higher-order photon gluon fusion process
- Also have the QCD – Compton process which probes quarks at the same order
- Both processes produce 2 angularly separated hard partons -> Di-jet
- At lower  $Q^2$ , resolved processes in which the photon assumes a hadronic structure begin to dominate
- Interested in the parton from the proton, would like to suppress the resolved component



# Direct Vs Resolved Processes

$$X_\gamma = \frac{1}{2E_{ey}} (p_{T1}e^{-\eta_1} + p_{T2}e^{-\eta_2})$$



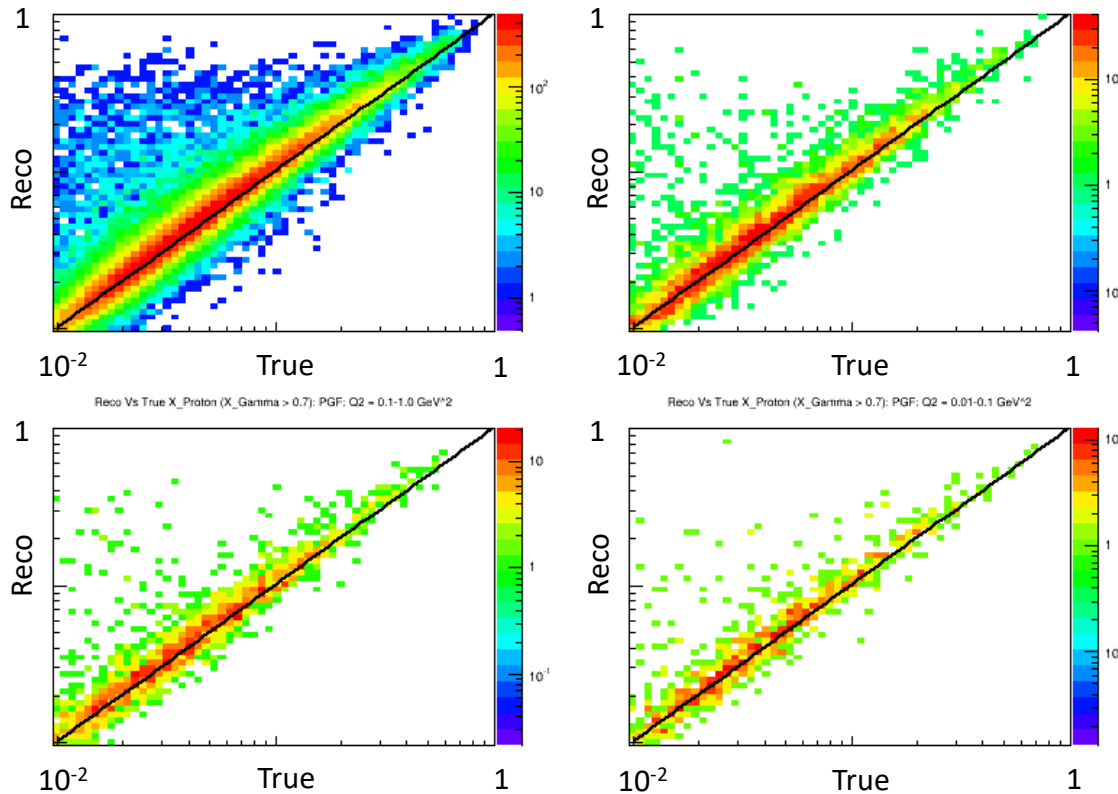
- Plot reconstructed  $X_\gamma$  for direct and resolved processes
- Direct processes should concentrate toward 1 while resolved processes are at lower values
- Direct processes dominate at higher  $Q^2$  while resolved are more prevalent at low  $Q^2$
- Cut of  $X_\gamma > 0.7$  enhances the direct fraction at all  $Q^2$

Accepted Region

# Proton Partonic Kinematics

Parton Momentum Fraction: Photon Gluon Fusion

- To measure gluon, need to probe the parton coming from the proton
- Momentum fraction of the parton from proton is well reconstructed



$$X_{q,g} = \frac{1}{2E_P} (p_{T1}e^{\eta_1} + p_{T2}e^{\eta_2})$$

# Proton Partonic Kinematics

$$X_{q,g} = x_B \left( 1 + \frac{M^2}{Q^2} \right)$$

- To measure gluon, need to probe the parton coming from the proton
- Momentum fraction of the parton from proton is well reconstructed
- $X_{q,g}$  is related to Bjorken- $x$  and  $Q^2$  at leading order



# Proton Partonic Kinematics

$$X_{q,g} = x_B \left( 1 + \frac{M^2}{Q^2} \right)$$

$$Q^2 = syx_B$$

- To measure gluon, need to probe the parton coming from the proton
- Momentum fraction of the parton from proton is well reconstructed
- $X_{q,g}$  is related to Bjorken- $x$  and  $Q^2$  at leading order
- $Q^2$  and Bjorken- $x$  are also related via the collision energy and inelasticity

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$$X_{q,g} = x_B + \frac{M^2}{sy}$$


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- Accessible  $X_{q,g}$  range basically determined by beam energies

# Proton Partonic Kinematics

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$$Q^2 = syx_B$$

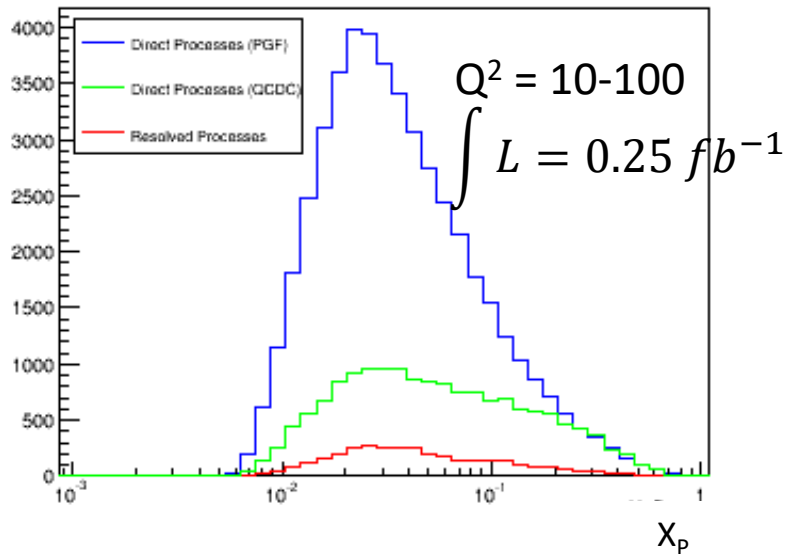
$$X_{q,g} = x_B + \frac{M^2}{sy}$$


$$\approx \frac{100}{(20000 \times 0.95)} \approx 0.005$$

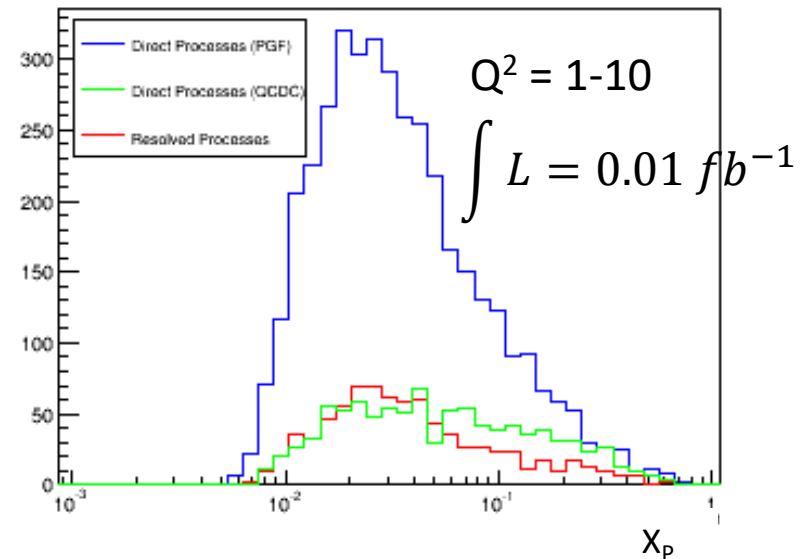
- To measure gluon, need to probe the parton coming from the proton
- Momentum fraction of the parton from proton is well reconstructed
- $X_{q,g}$  is related to Bjorken-x and  $Q^2$  at leading order
- $Q^2$  and Bjorken-x are also related via the collision energy and inelasticity
- Accessible  $X_{q,g}$  range basically determined by beam energies
- Lowest  $X_{q,g}$  we can probe is about 0.005

# $X_{q,g}$ For Different $Q^2$

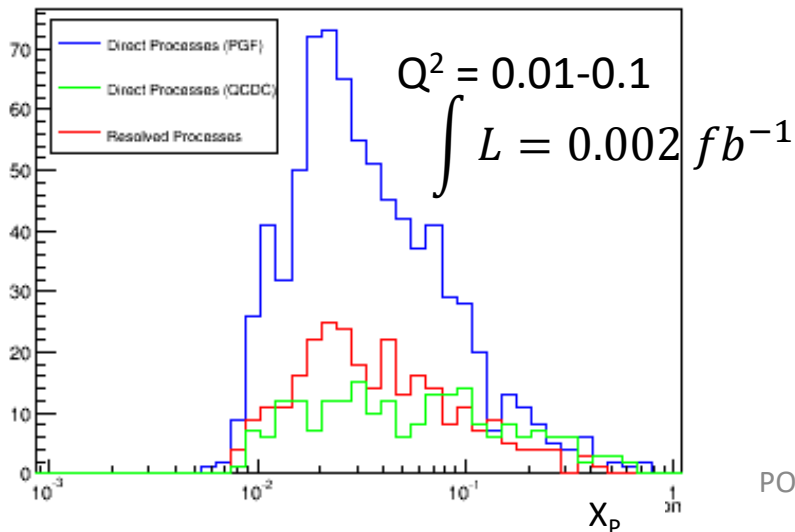
Reco X Proton ( $X_{\text{Gamma}} > 0.7$ ):  $Q^2 = 10-100$



Reco X Proton ( $X_{\text{Gamma}} > 0.7$ ):  $Q^2 = 1-10$



Reco X Proton ( $X_{\text{Gamma}} > 0.7$ ):  $Q^2 = 0.01-0.1$



- At lower  $Q^2$ , contribution from resolved process increases while QCD Compton contribution decreases
- For a given di-jet mass range, same  $X_{q,g}$  can be probed over large range of  $Q^2$
- Can test evolution of gluons

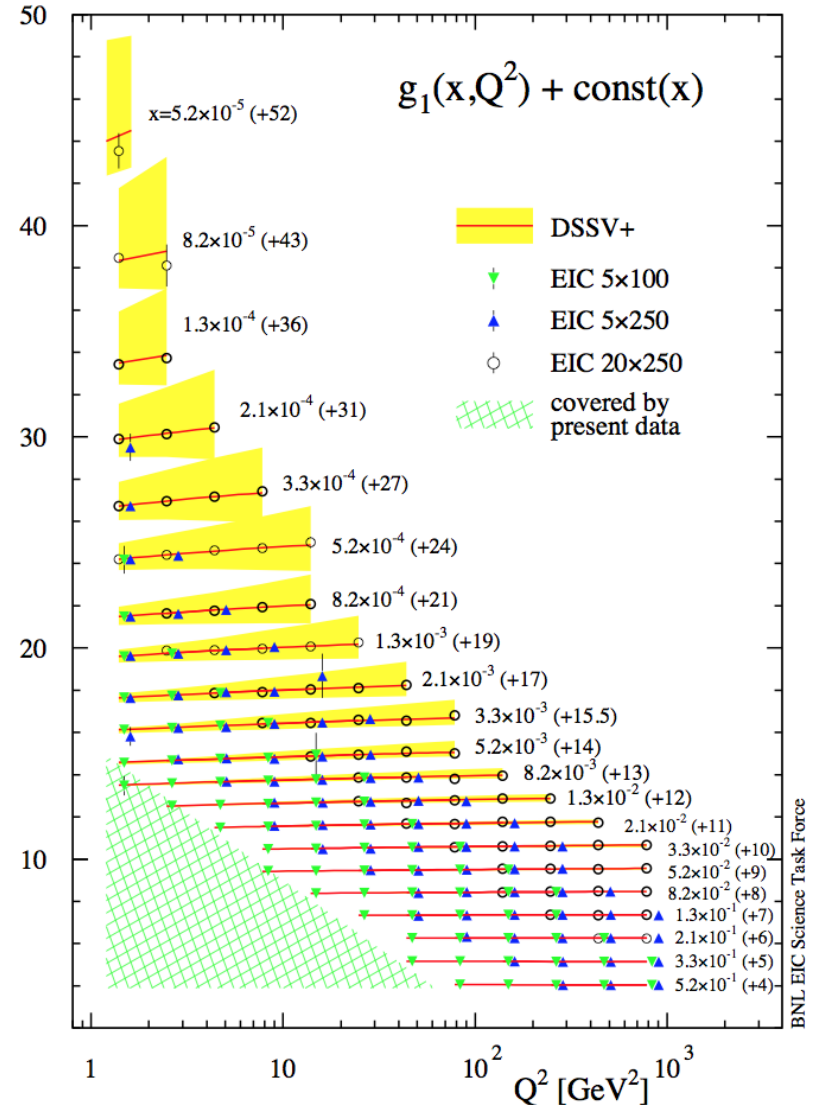
# Accessing $\Delta G$

- Several observables are sensitive to  $\Delta G$  in DIS but golden measurement at an EIC would be scaling violation of  $g_1(x, Q^2)$

$$\frac{dg_1(x, Q^2)}{d\ln(Q^2)} \approx -\Delta g(x, Q^2)$$

- Current DIS constraints on  $\Delta G$  hampered by limited  $x$  &  $Q^2$  coverage
- EIC would greatly expand kinematic reach and precision of  $g_1(x, Q^2)$  measurements!

arXiv:1206.6014

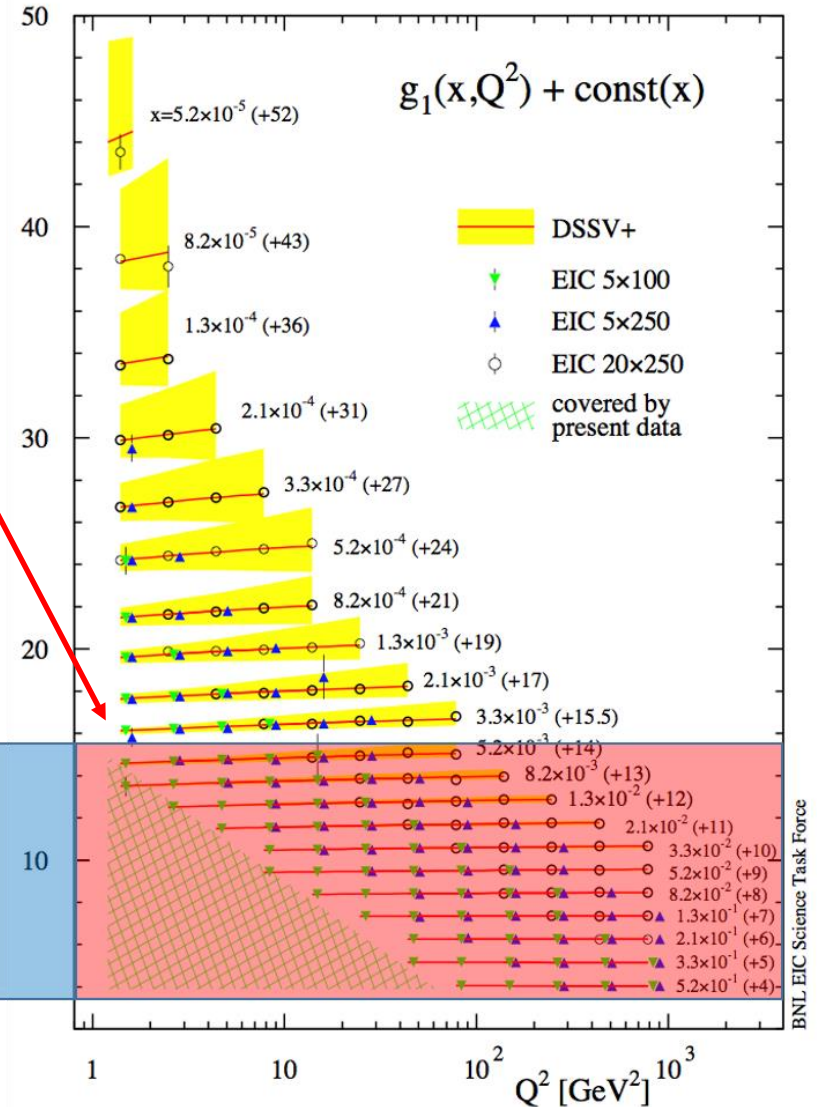


# Accessing $\Delta G$

- PGF di-jet asymmetry measurements will provide alternative access to  $\Delta G$

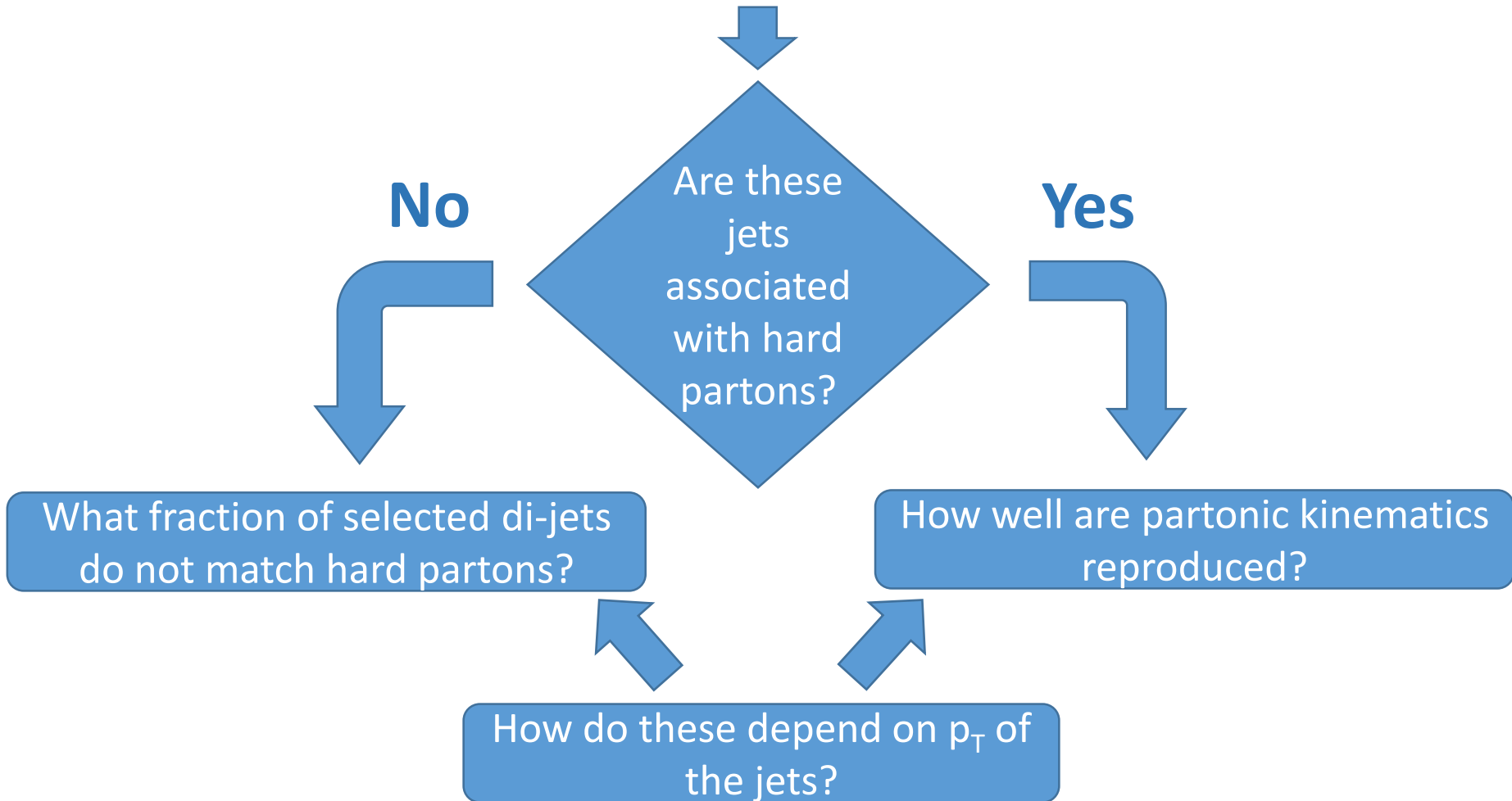
$Q^2$  and  $x$  range covered by di-jet asymmetry measurements

Experimentally possible to extend these measurements to  $Q^2 < 1$

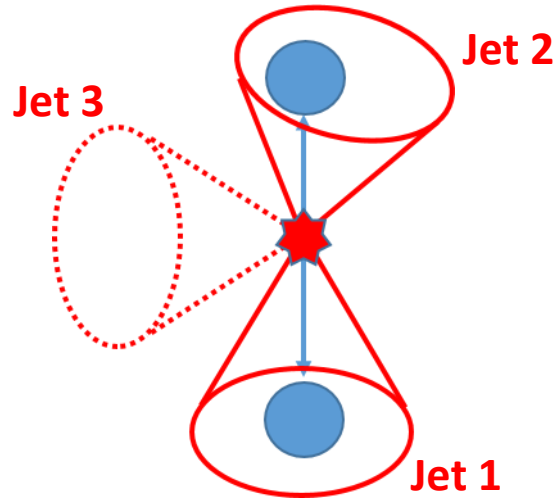


# How Low Can We Go?

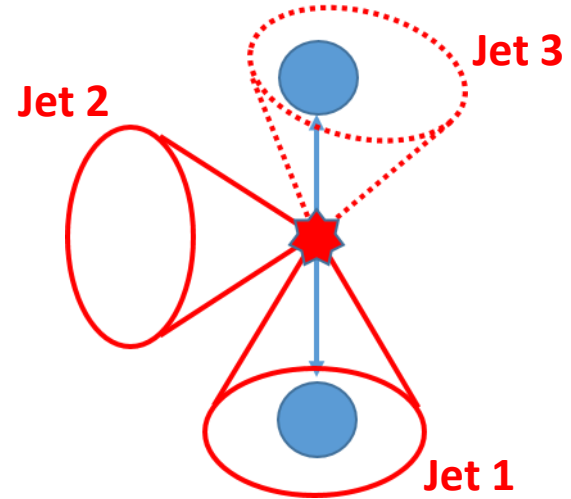
Select di-jets by finding two highest  $p_T$  jets in event and requiring they be separated in azimuth



# Matching Fractions: $Q^2 = 0.01\text{-}0.1 \text{ GeV}$



“Matched Event”



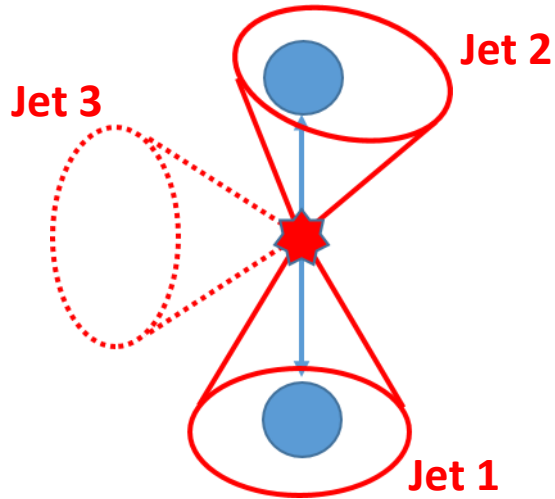
“UnMatched Event”

| Jet $p_T$ Ranges                 | % of <b>PGF</b> / <b>Resolved</b> Events Captured | Of Captured: % <b>PGF</b> / <b>Resolved</b> Matched |
|----------------------------------|---|---|
| Hi Jet > 5 GeV && Lo Jet > 4 GeV | 1% / <1%  | 87% / 83%   |
| Hi Jet < 5 GeV    Lo Jet < 4 GeV | 25% / 19%   | 70% / 69%   |

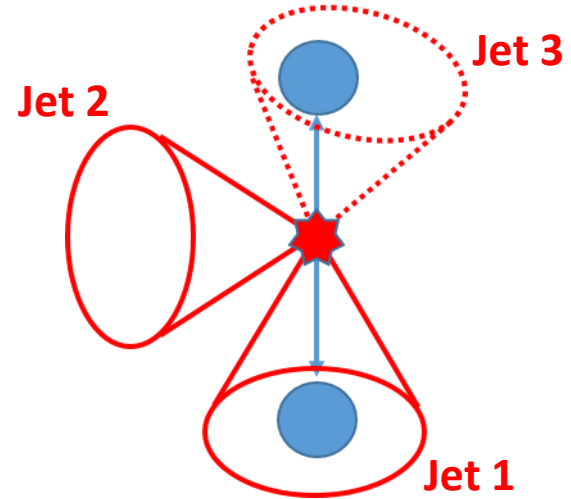
(Still require Hi Jet > 2 && Lo Jet > 1 GeV) POETIC - 2016



# Matching Fractions: $Q^2 = 10\text{-}100\text{ GeV}$



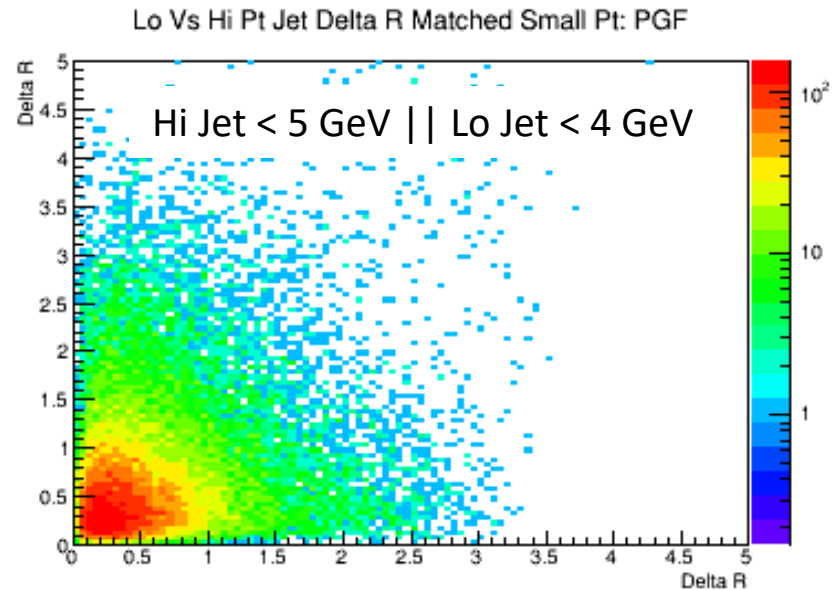
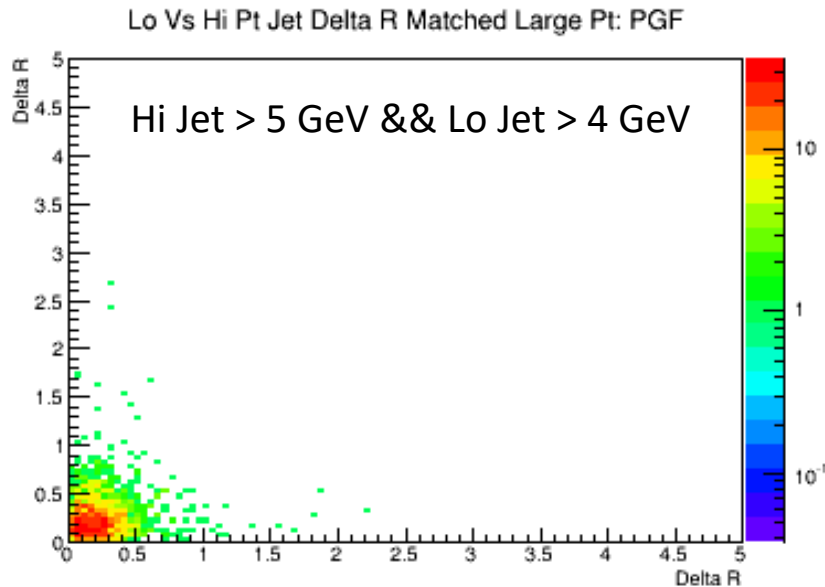
“Matched Event”



“UnMatched Event”

| Jet $p_T$ Ranges                 | % of <b>PGF</b> / <b>Resolved</b> Events Captured | Of Captured: % <b>PGF</b> / <b>Resolved</b> Matched |
|----------------------------------|---|---|
| Hi Jet > 5 GeV && Lo Jet > 4 GeV | 35% / 11%   | 91% / 91%   |
| Hi Jet < 5 GeV    Lo Jet < 4 GeV | 60% / 44%   | 83% / 73%   |

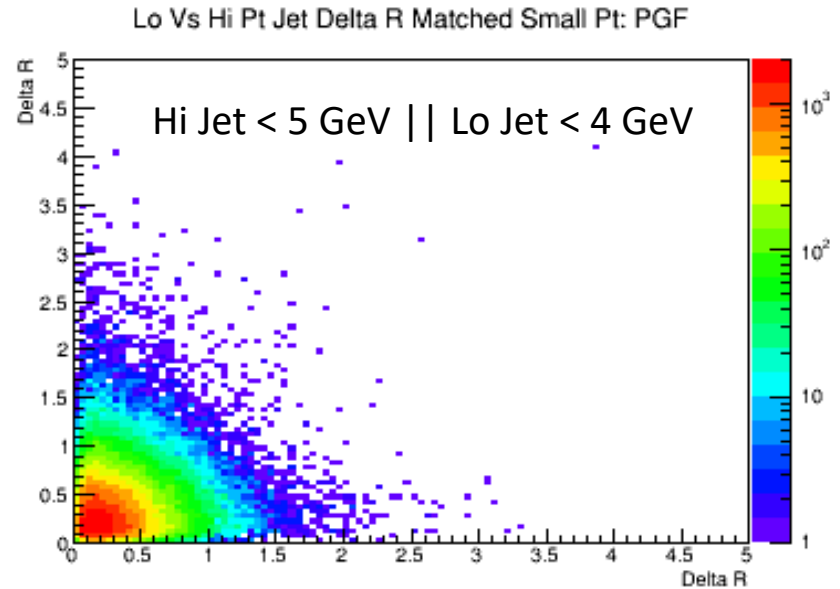
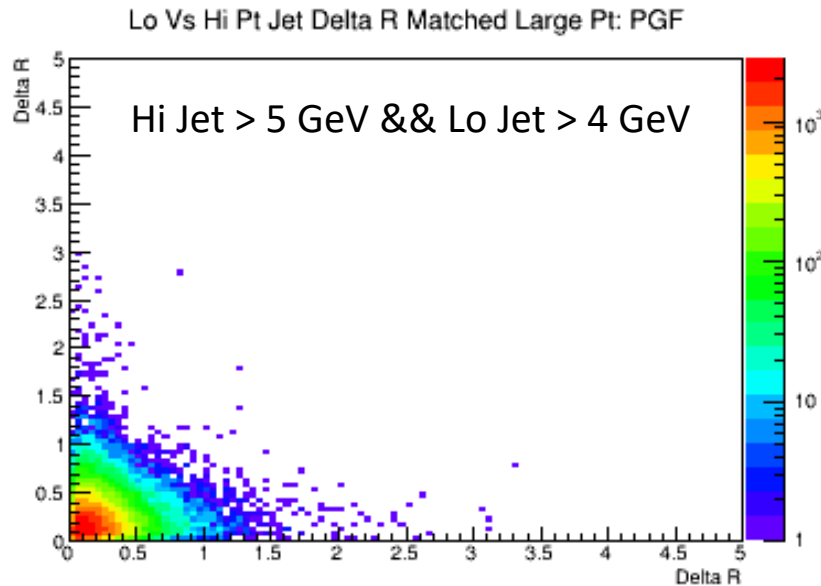
# PGF $\Delta R$ : $Q^2 = 0.01 - 0.1 \text{ GeV}^2$



$$\Delta R = \sqrt{(y_{part} - y_{jet})^2 + (\varphi_{part} - \varphi_{jet})^2}$$

- For matched events, plot  $\Delta R$  for both jets
- Do this for high and low  $p_T$  jets separately
- See that  $\Delta R$  values are somewhat larger for low  $p_T$  jets – indicates poorer matching

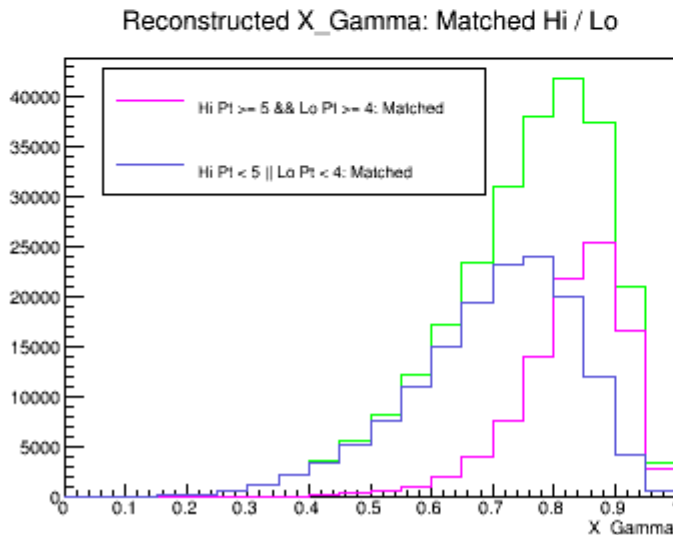
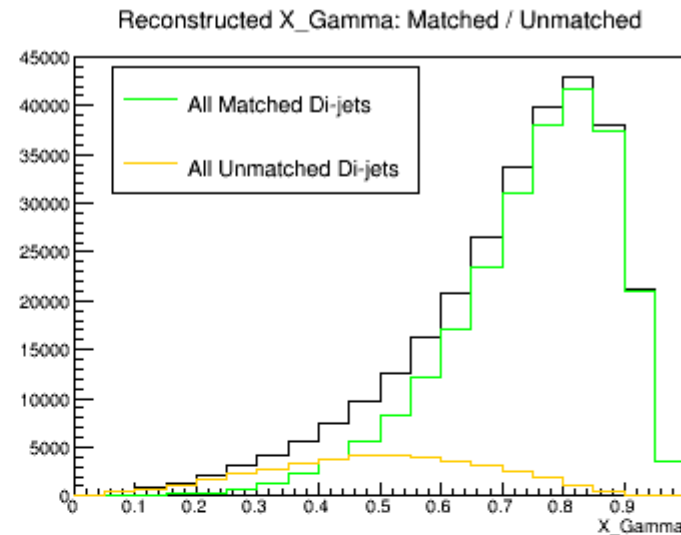
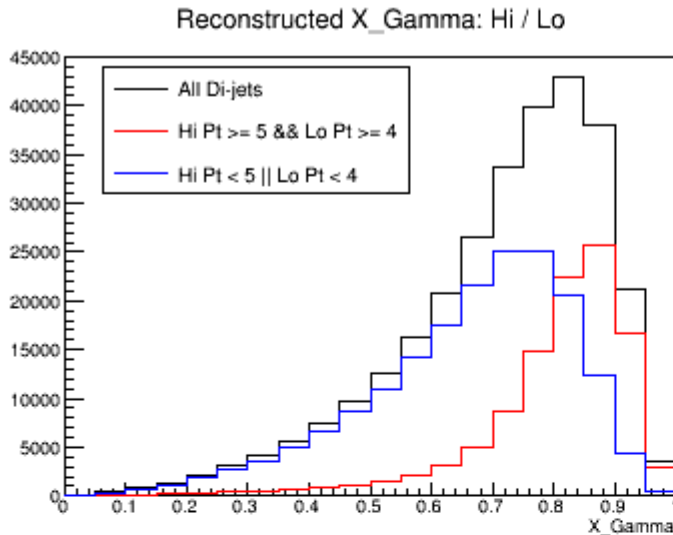
# PGF $\Delta R$ : $Q^2 = 10 - 100 \text{ GeV}^2$



$$\Delta R = \sqrt{(y_{part} - y_{jet})^2 + (\varphi_{part} - \varphi_{jet})^2}$$

- The difference in  $\Delta R$  behavior between low and high jet  $p_T$  is much greater at lower values of  $Q^2$
- Similar results seen for other subprocesses

# $X_\gamma$ Reproduction: $Q^2 = 10 - 100 \text{ GeV}^2$



- How does the reproduction of  $X_\gamma$  depend on jet  $p_T$ ?
- As expected unmatched events do not reproduce  $X_\gamma$  well
- See that high  $p_T$  range is more peaked toward 1 even for matched events

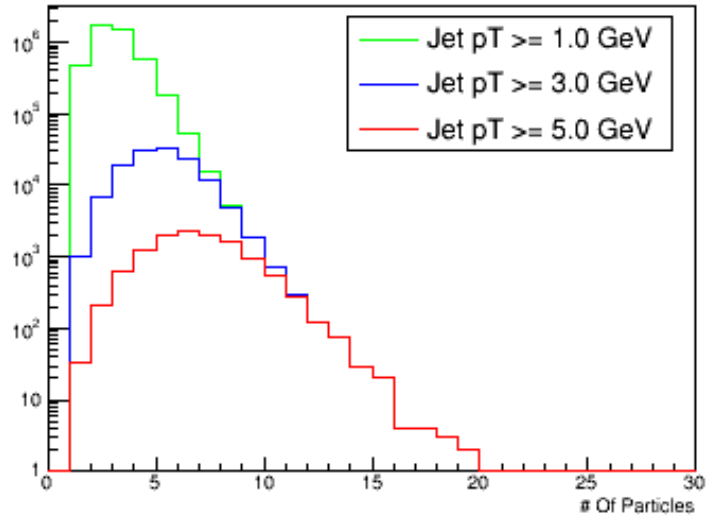
# Conclusions

- Basic jet parameters: Larger radius leads to more jets and more particles in jet, higher  $p_T$  jets have more particles but lower multiplicity. Not much dependence on jet algorithm
- Di-jet measurements from photon-gluon fusion subprocess will provide important cross check to gluon polarization measurements from  $g_1$  scaling violations
- Correlation between jet and parton breaks down as jet  $p_T$  decreases meaning higher  $p_T$  jets are better for reconstructing the initial kinematics

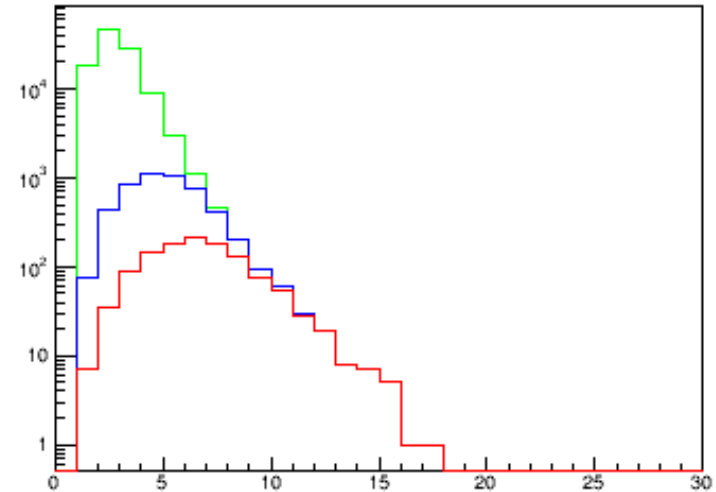
# Backup

# Jet Particle Mult: $Q^2 = 0.01 - 0.1 \text{ GeV}^2$

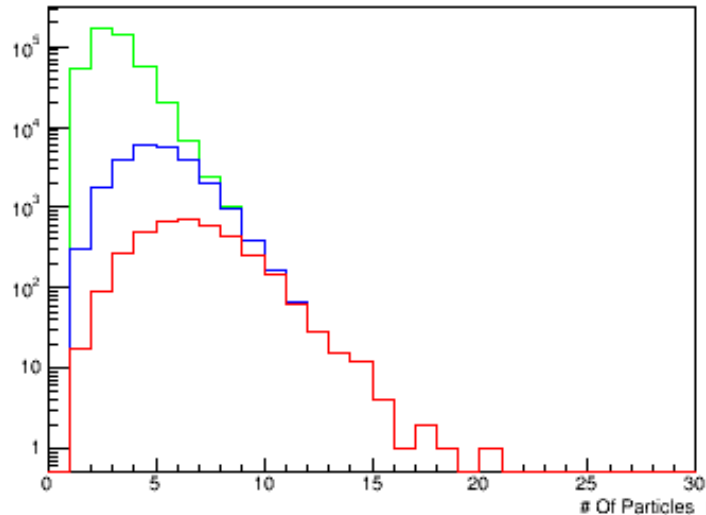
# Jet Particles: Resolved



# Jet Particles: QCD



# Jet Particles: PGF

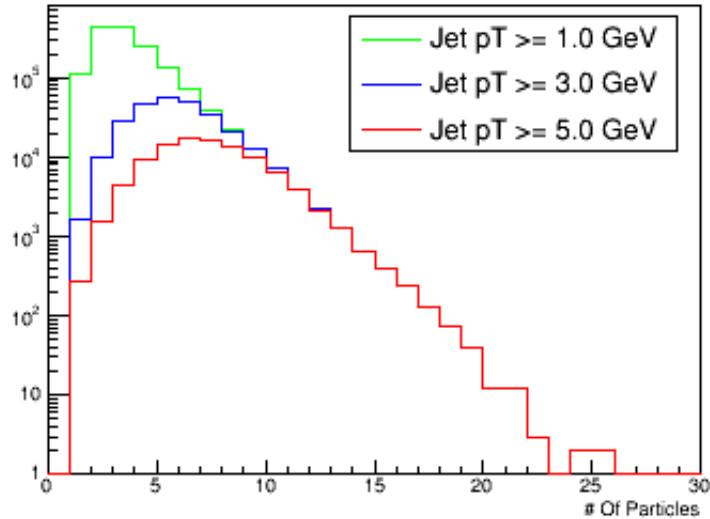


# Jet Particles: L.O. DIS

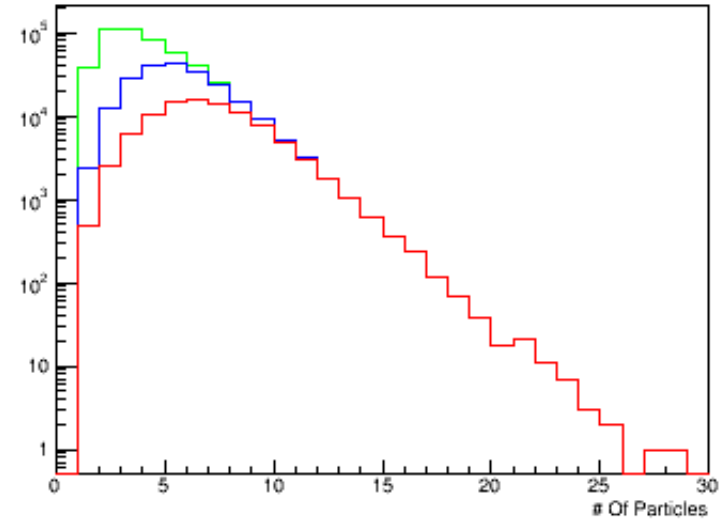
- Same as previous slide but for lower  $Q^2$  range
- Median numbers of particles stay roughly the same as higher  $Q^2$  case but frequency of jets with high number of particles down sharply

# Jet Particle Mult: $Q^2 = 10 - 100 \text{ GeV}^2$

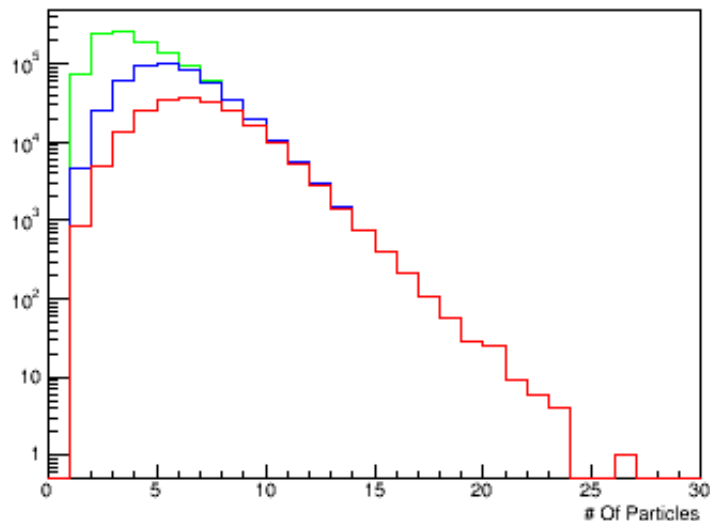
# Jet Particles: Resolved



# Jet Particles: QCD



# Jet Particles: PGF



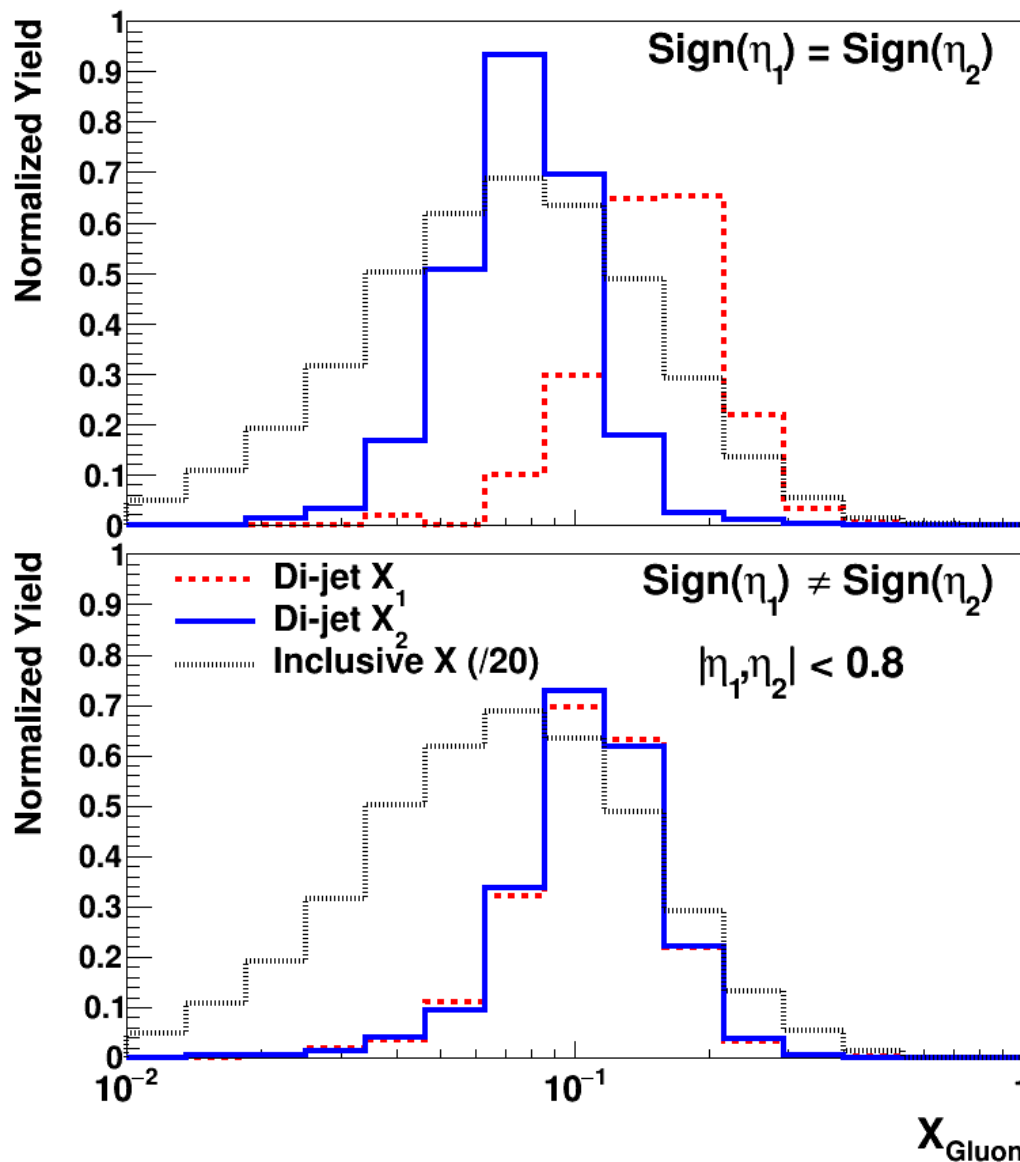
- Number of particles in a jet for 3 minimum jet  $p_T$  values
- Increase in minimum jet  $p_T$  leads to increase in average number of particles in jet
- Higher  $p_T$  jets  $\rightarrow$  more “jet like” than “single particle like”



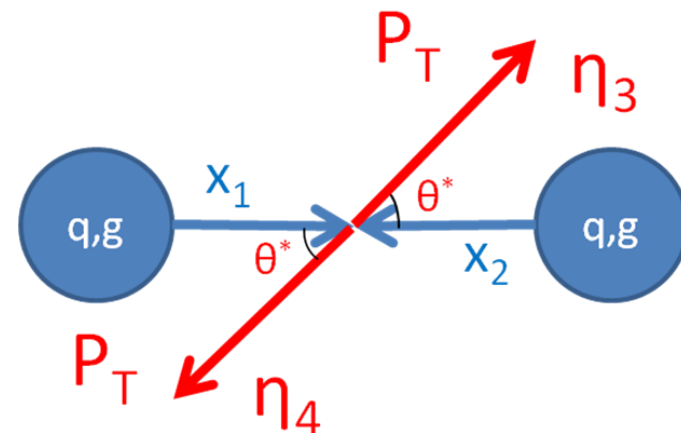
# Jet Basics: Frames

- Can define several useful frames:
  - Lab: Detector-based frame
  - Hadron-Boson: Beam hadron is at rest, z-direction chosen along virtual photon momentum vector
  - Breit: Virtual photon moves in -z direction and boost such that it has zero energy. Separation into target and remnant regions
  - Center of Mass: Virtual photon and struck parton have equal and opposite momenta. Can define Feynman-x

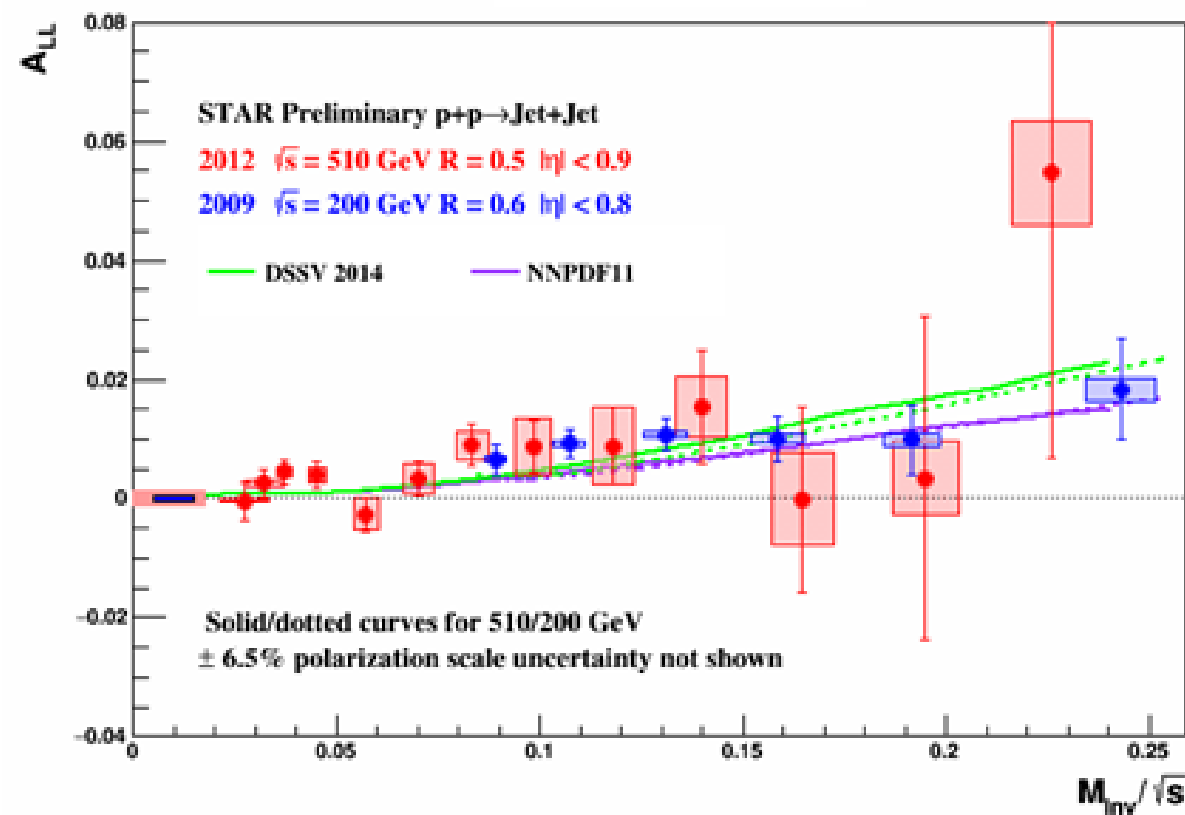
# Di-jet $A_{LL}$ (pp)



- Coincidence measurements capture more information about hard scatter and better constrain initial kinematics



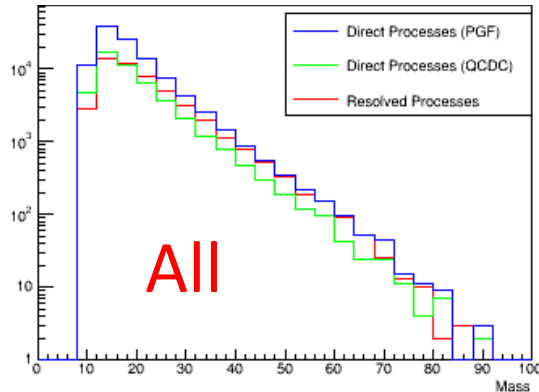
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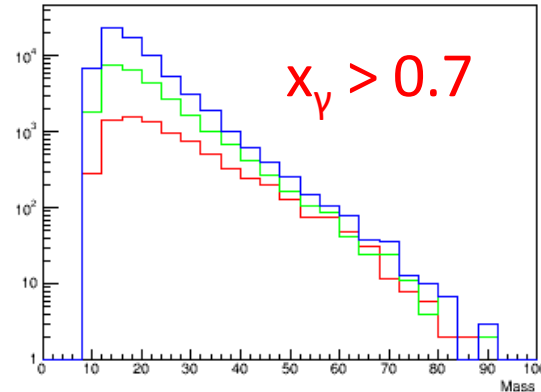
- Coincidence measurements capture more information about hard scatter and better constrain initial kinematics
- Di-jet  $A_{LL}$  plotted vs  $M_{inv}/\sqrt{s}$  ( $\sim \sqrt{x_1 x_2}$  at L.O.) for data taken at  $\sqrt{s} = 200$  and  $510$  GeV
- 510 GeV data extend to lower  $M_{inv}/\sqrt{s}$  (lower  $x$ ) where  $\Delta G$  not as well constrained while 200 GeV data give better precision at mid to high  $M_{inv}/\sqrt{s}$

# Di-jet Invariant Mass

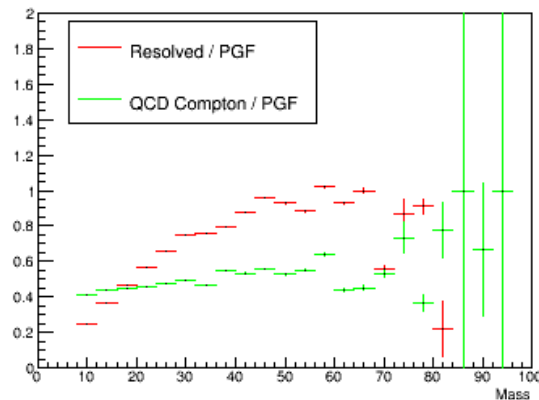
Di-jet Mass:  $Q^2 = 10-100$



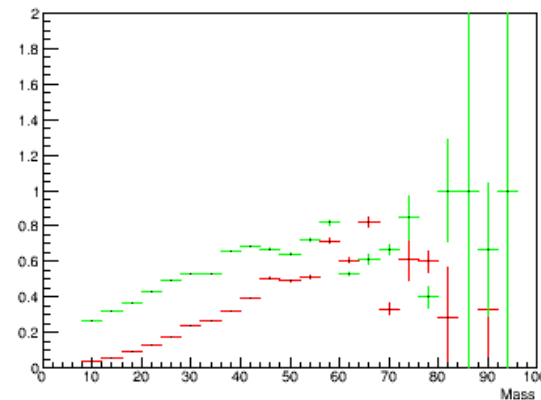
Di-jet Mass:  $Q^2 = 10-100$



Subprocess Ratio Vs Mass:  $Q^2 = 10-100$



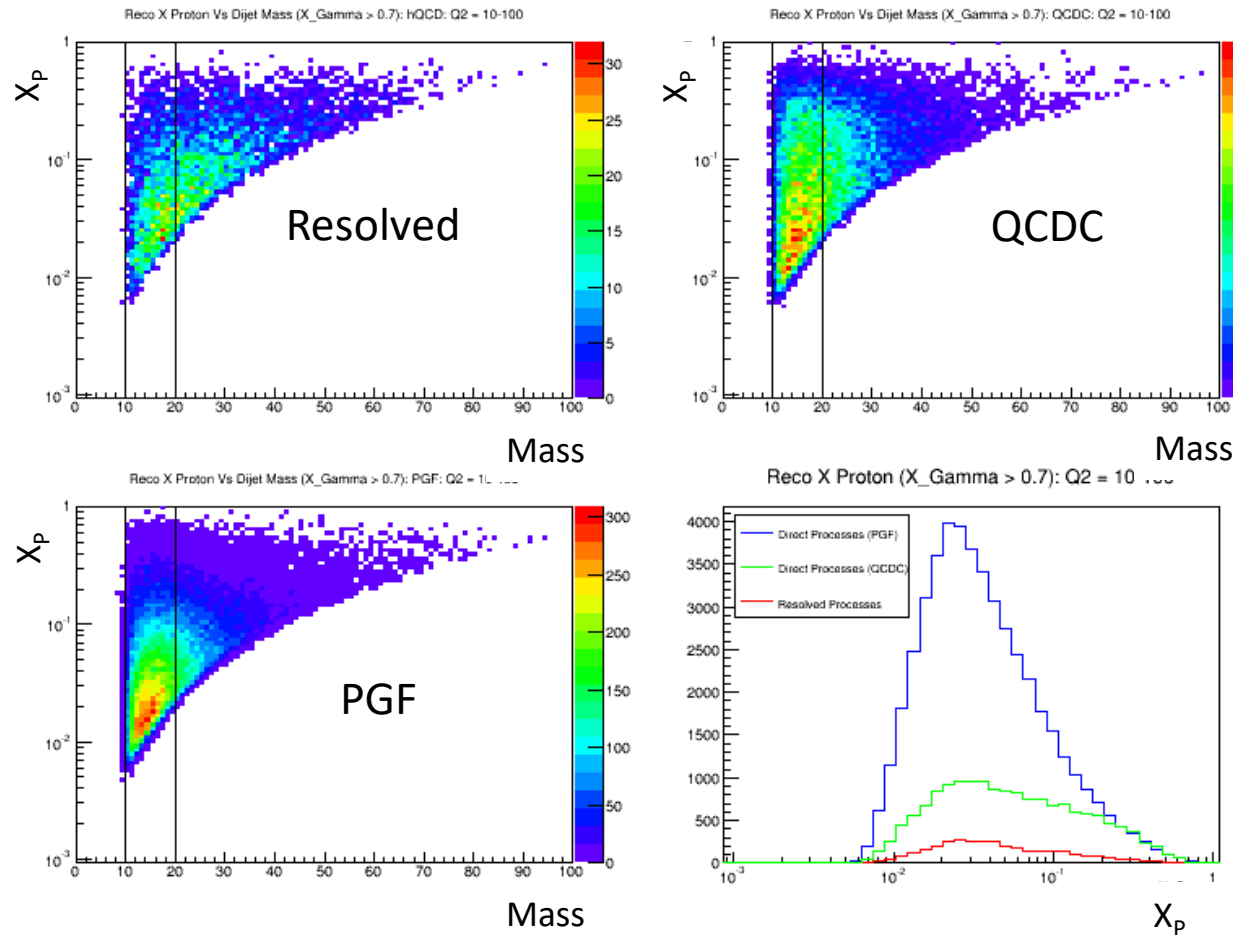
Subprocess Ratio Vs Mass ( $X_\gamma > 0.7$ ):  $Q^2 = 10-100$



- See that the cut on  $X_\gamma$  significantly reduces the resolved contribution while maintaining the direct events
- Separation between resolved and direct is most prominent at high  $Q^2$  and low di-jet invariant mass

# $X_{q,g}$ Vs Mass

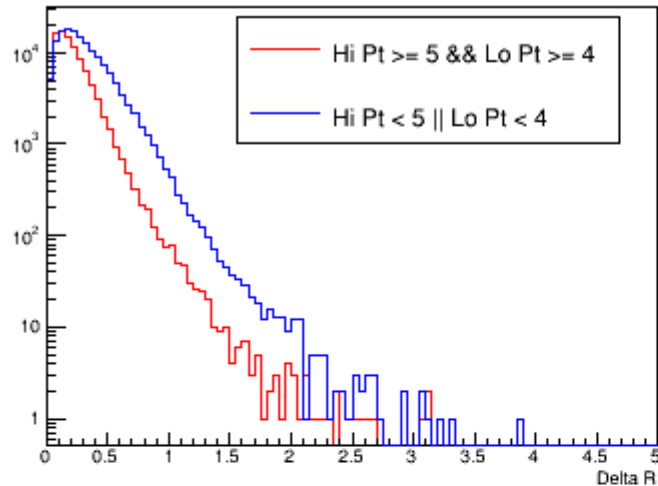
$$Q^2 = 10 - 100 \text{ GeV}/c^2$$



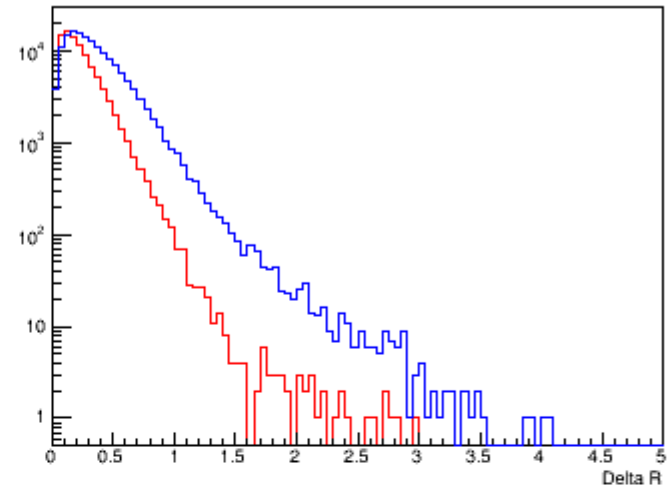
- As shown on the previous slide, accessible  $X_{q,g}$  range is determined largely by beam energy
- Different di-jet mass ranges select different process fractions with lower masses containing less resolved contribution
- Selection of high mass events also cut out low  $X_{q,g}$  contribution

# Partonic Matching: Shape Comparison

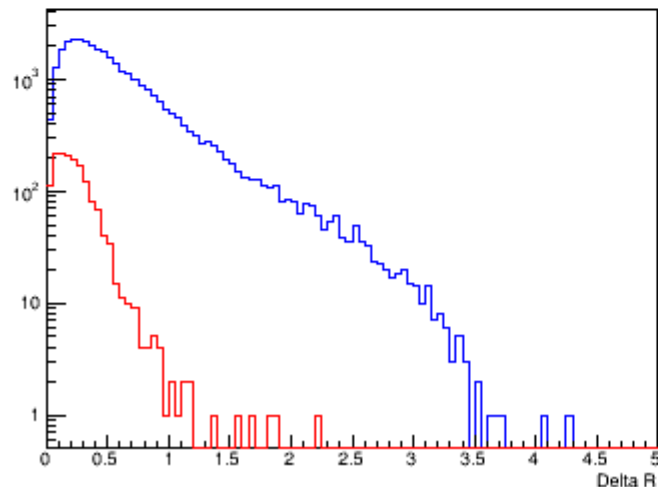
Matched Leading Jet Delta R: PGF: Q2 = 10 - 100 GeV2



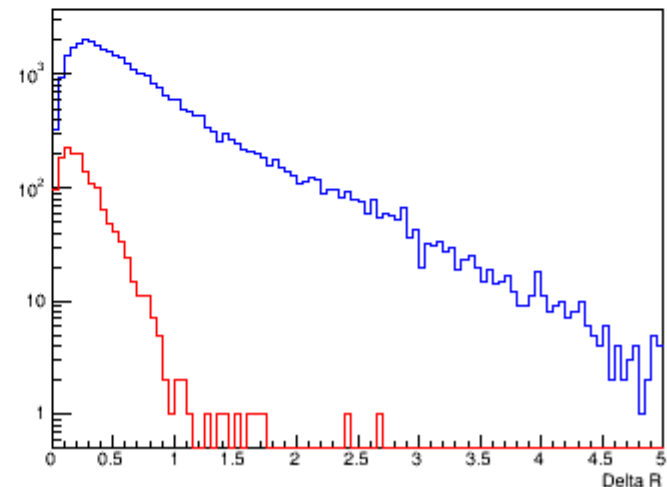
Matched Sub-Leading Jet Delta R: PGF: Q2 = 10 - 100 GeV2



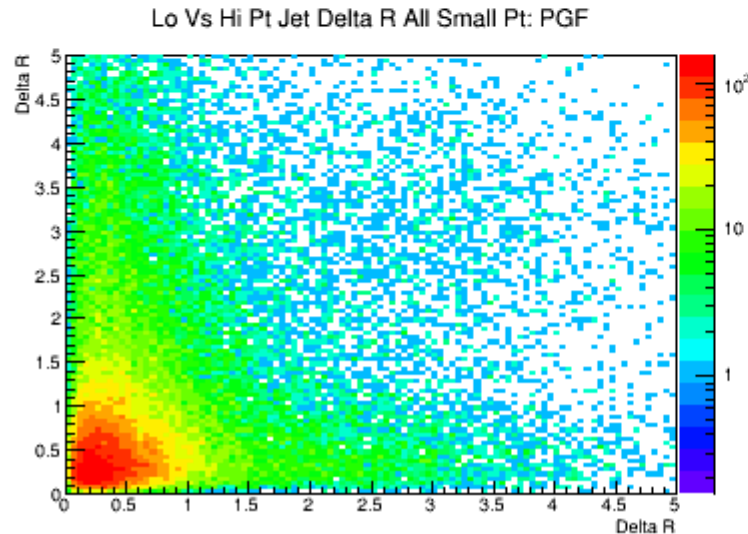
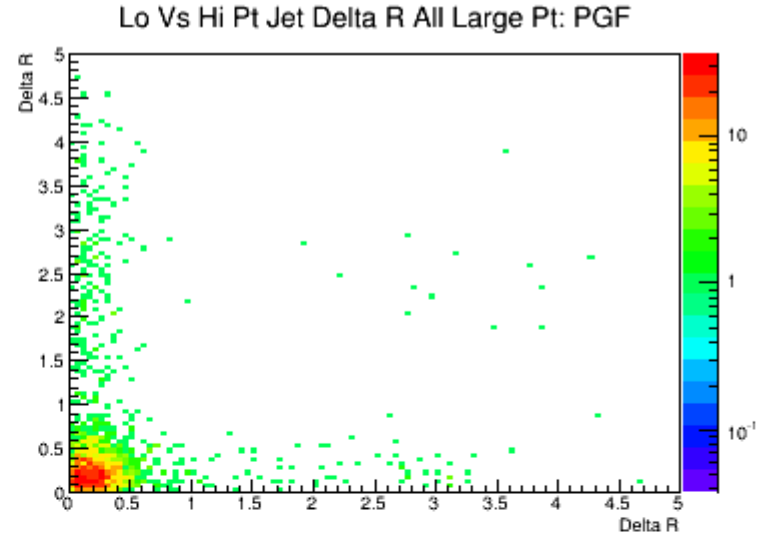
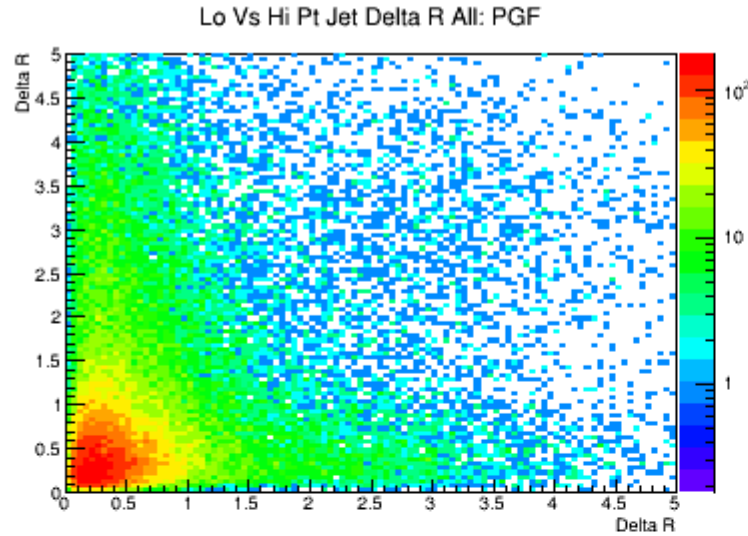
Matched Leading Jet Delta R: PGF: Q2 = 0.01 - 0.1 GeV2



Matched Sub-Leading Jet Delta R: PGF: Q2 = 0.01 - 0.1 GeV2

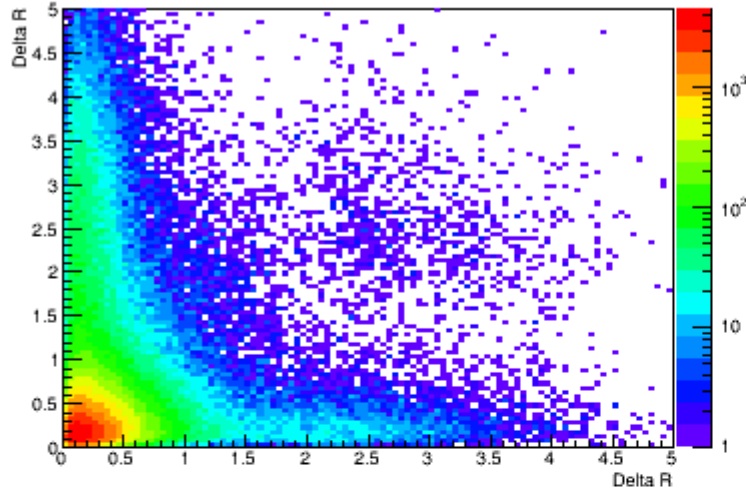


# Partonic Matching: PGF Q2 = 0.01 – 0.1

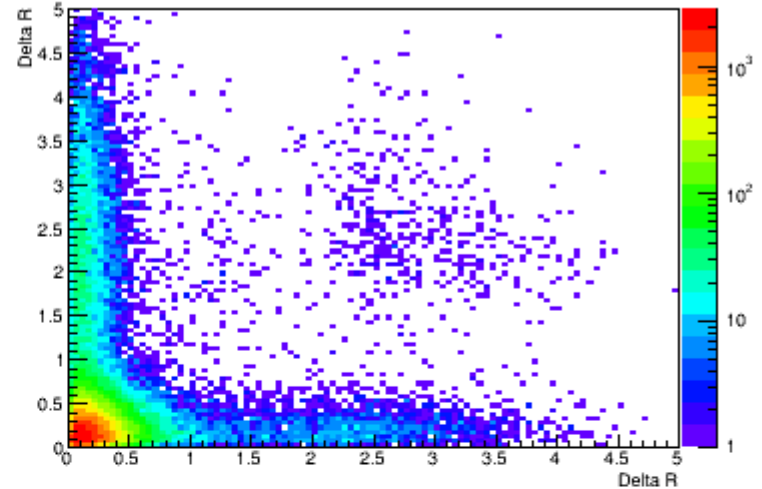


# Partonic Matching: PGF Q2 = 10 - 100

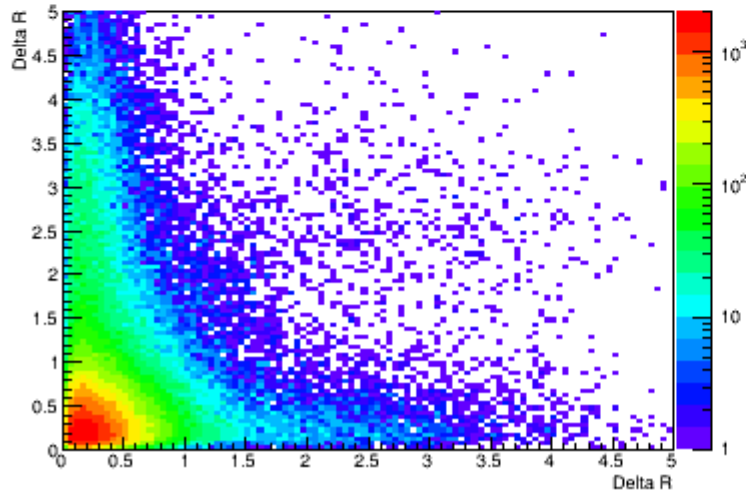
Lo Vs Hi Pt Jet Delta R All: PGF



Lo Vs Hi Pt Jet Delta R All Large Pt: PGF



Lo Vs Hi Pt Jet Delta R All Small Pt: PGF





# $X_\gamma$ Reproduction: $Q^2 = 0.01 - 0.1 \text{ GeV}^2$

